

## Graphing Circles & Lines

**Standard Form of a Circle:**  $(x-h)^2 + (y-k)^2 = r^2$

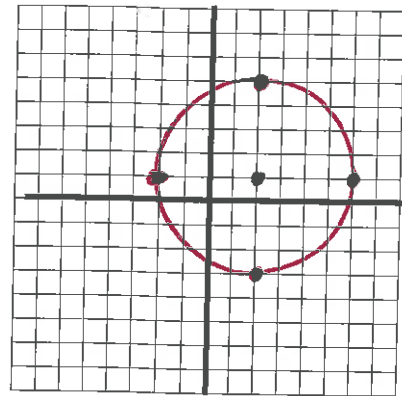
$(h,k)$  is the Center                       $r$  is the radius.

1  $(x-2)^2 + (y-1)^2 = 16$

**a. Find Center & Radius**

Center is  $(2, 1)$   
radius is  $\sqrt{16}$  or 4.

**b. Graph (use a Compass!)**



2  $(x+3)^2 + y^2 = 12$

Find the center and radius.

Center is  $(-3, 0)$

radius =  $\sqrt{12}$

think of as:  $(x - (-3))^2$

↑  
Double  
negative  
make a +

3. center =  $(6, -2)$

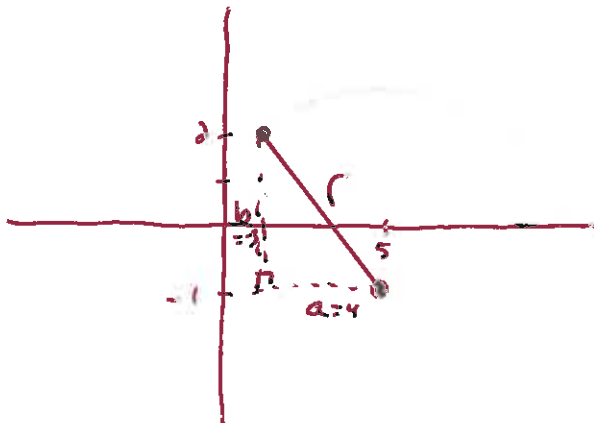
Radius = 5

Write the equation of the circle in standard form.

$$(x-6)^2 + (y - (-2))^2 = 5^2$$

$$(x-6)^2 + (y+2)^2 = 25$$

4. Find the standard form a circle centered at  $(5, -1)$  and passing through the point  $(1, 2)$ .



$$a^2 + b^2 = r^2$$

$$(5-1)^2 + (-1-2)^2 = r^2$$

$$4^2 + (-3)^2 = r^2$$

$$16 + 9 = r^2$$

$$r^2 = 25$$

$$r = 5$$

$$(x-5)^2 + (y+1)^2 = 25$$

## Completing the Square to find Standard Form:

Steps	$x^2 + y^2 + 4x - 2y - 11 = 0$
<b>a. Sort the equation</b> - put x's together - put y's together - move constant to other side	$x^2 + 4x + y^2 - 2y = 11$
<b>b. Complete the Square</b> - Add $(1/2 \text{ x-term})^2$ to both sides - Add $(1/2 \text{ y-term})^2$ to both sides	$x^2 + 4x + (2)^2 + y^2 - 2y + (-1)^2 = 11 + (2)^2 + (-1)^2$ $x^2 + 4x + 4 + y^2 - 2y + 1 = 16$
<b>c. Write in factored form</b> - the $(1/2 \text{ x-term})$ and $(1/2 \text{ y-term})$ always end up inside the ( )'s.	$(x+2)(x+2) + (y-1)(y-1) = 16$ $(x+2)^2 + (y-1)^2 = 16$

### 5. Find the standard form of each circle. State the Center and Radius of each.

a.  $x^2 + y^2 - 8x + 12y + 43 = 0$

b.  $x^2 + y^2 - 14x + 24 = 0$

$$x^2 - 8x + y^2 + 12y = -43$$

$$x^2 - 8x + (-4)^2 + y^2 + 12y + (6)^2 = -43 + (-4)^2 + (6)^2$$

$$(x-4)^2 + (y+6)^2 = 9$$

Center =  $(4, -6)$

$r = 3$

b.)  $x^2 - 14x + y^2 = -24$

$$x^2 - 14x + (-7)^2 + y^2 + (0)^2 = -24 + (-7)^2 + (0)^2$$

$$(x-7)^2 + (y-0)^2 = 25$$

$$(x-7)^2 + y^2 = 25$$

Center =  $(7, 0)$

$r = 5$

## Graphing a Line:

6.  $-4x - 8y = 16$

a. Put in  $y=mx+b$  form

$$-4x - 8y = 16$$

$$-8y = 4x + 16$$

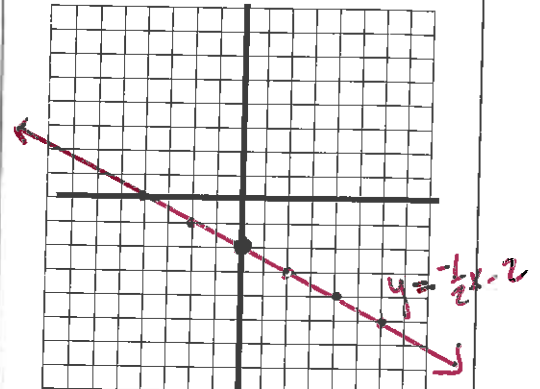
$$y = -\frac{1}{2}x - 2$$

b. Find slope & intercept

$$\text{Slope} = -\frac{1}{2} \quad \begin{array}{l} \text{Down} \\ \text{Right} \end{array}$$

$$y\text{-int} = -2$$

3. Graph



## Solving a system by graphing:

7. Solve by Graphing

$$25 = (x+1)^2 + y^2$$

$$y + x = -2$$

Circle

$$25 = (x+1)^2 + y^2$$

Center  $(-1, 0)$

$$r = 5$$

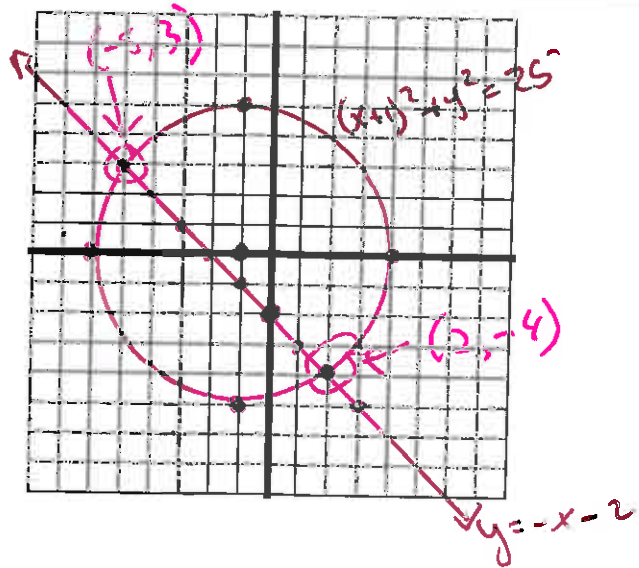
Line:

$$y + x = -2$$

$$y = -x - 2$$

$$\text{Slope} = -\frac{1}{1}$$

$$b = -2$$



Solutions:

$(-5, 3)$  and  $(2, -4)$

